$$\frac{d}{dx}\cot x = -\csc^2 x = \frac{-1}{\sin^2 x}$$