$$\frac{d}{dx}|x| = \frac{|x|}{x} = \operatorname{sgn} x, \qquad x \neq 0$$