$$\frac{1}{R}\left[\int_0^R \frac{2mL}{\sqrt{(L^2+r^2)^3}}dr\right]$$