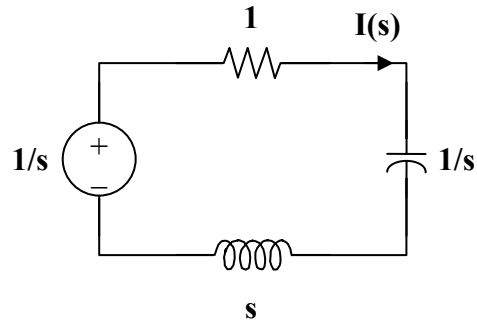


Chapter 16, Solution 1.

Consider the s-domain form of the circuit which is shown below.

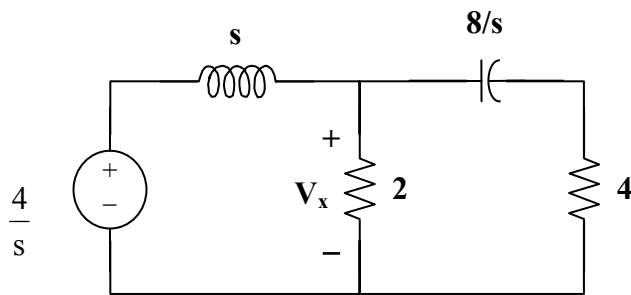


$$I(s) = \frac{1/s}{1 + s + 1/s} = \frac{1}{s^2 + s + 1} = \frac{1}{(s + 1/2)^2 + (\sqrt{3}/2)^2}$$

$$i(t) = \frac{2}{\sqrt{3}} e^{-t/2} \sin\left(\frac{\sqrt{3}}{2} t\right)$$

$$i(t) = \underline{\underline{1.155 e^{-0.5t} \sin(0.866t) \text{ A}}}$$

Chapter 16, Solution 2.



$$\frac{V_x - \frac{4}{s}}{s} + \frac{V_x - 0}{2} + \frac{V_x - 0}{4 + \frac{8}{s}} = 0$$

$$V_x(4s + 8) - \frac{(16s + 32)}{s} + (2s^2 + 4s)V_x + s^2V_x = 0$$

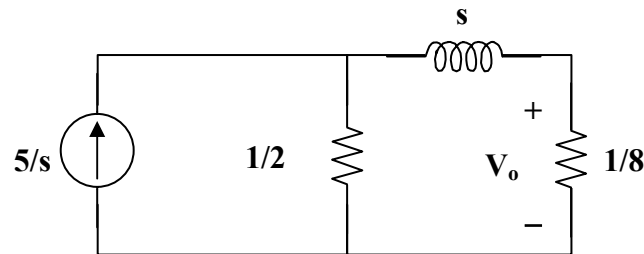
$$V_x(3s^2 + 8s + 8) = \frac{16s + 32}{s}$$

$$V_x = -16 \frac{s + 2}{s(3s^2 + 8s + 8)} = -16 \left(\frac{0.25}{s} + \frac{-0.125}{s + \frac{4}{3} + j\frac{\sqrt{8}}{3}} + \frac{-0.125}{s + \frac{4}{3} - j\frac{\sqrt{8}}{3}} \right)$$

$$v_x = \underline{(-4 + 2e^{-(1.3333 + j0.9428)t} + 2e^{-(1.3333 - j0.9428)t})u(t) \text{ V}}$$

$$v_x = \underline{4u(t) - e^{-4t/3} \cos\left(\frac{2\sqrt{2}}{3}t\right) - \frac{6}{\sqrt{2}}e^{-4t/3} \sin\left(\frac{2\sqrt{2}}{3}t\right) \text{ V}}$$

Chapter 16, Solution 3.



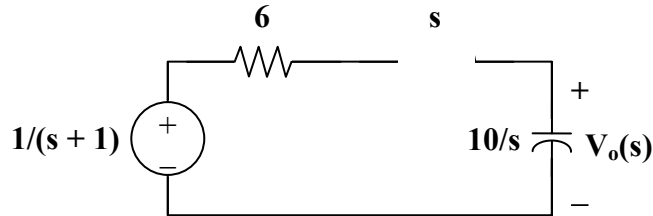
Current division leads to:

$$V_o = \frac{1}{8} \frac{5}{s} \left(\frac{\frac{1}{2}}{\frac{1}{2} + \frac{1}{8} + s} \right) = \frac{5}{10 + 16s} = \frac{5}{16(s + 0.625)}$$

$$v_o(t) = \underline{0.3125(1 - e^{-0.625t})u(t) \text{ V}}$$

Chapter 16, Solution 4.

The s-domain form of the circuit is shown below.



Using voltage division,

$$V_o(s) = \frac{10/s}{s+6+10/s} \left(\frac{1}{s+1} \right) = \frac{10}{s^2+6s+10} \left(\frac{1}{s+1} \right)$$

$$V_o(s) = \frac{10}{(s+1)(s^2+6s+10)} = \frac{A}{s+1} + \frac{Bs+C}{s^2+6s+10}$$

$$10 = A(s^2+6s+10) + B(s^2+s) + C(s+1)$$

Equating coefficients :

$$s^2: \quad 0 = A + B \quad \longrightarrow \quad B = -A$$

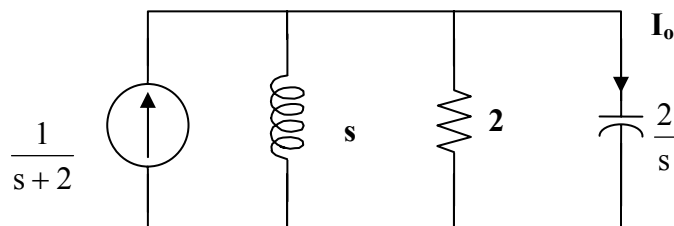
$$s^1: \quad 0 = 6A + B + C = 5A + C \quad \longrightarrow \quad C = -5A$$

$$s^0: \quad 10 = 10A + C = 5A \quad \longrightarrow \quad A = 2, B = -2, C = -10$$

$$V_o(s) = \frac{2}{s+1} - \frac{2s+10}{s^2+6s+10} = \frac{2}{s+1} - \frac{2(s+3)}{(s+3)^2+1^2} - \frac{4}{(s+3)^2+1^2}$$

$$v_o(t) = \underline{2e^{-t} - 2e^{-3t} \cos(t) - 4e^{-3t} \sin(t) \text{ V}}$$

Chapter 16, Solution 5.



$$V = \frac{1}{s+2} \left(\frac{1}{\frac{1}{s} + \frac{1}{2} + \frac{s}{2}} \right) = \frac{1}{s+2} \left(\frac{2s}{s^2 + s + 2} \right) = \frac{2s}{(s+2)(s+0.5 + j1.3229)(s+0.5 - j1.3229)}$$

$$I_o = \frac{Vs}{2} = \frac{s^2}{(s+2)(s+0.5 + j1.3229)(s+0.5 - j1.3229)}$$

$$= \frac{1}{s+2} + \frac{(-0.5 - j1.3229)^2}{(1.5 - j1.3229)(-j2.646)} \frac{(-0.5 + j1.3229)^2}{(1.5 + j1.3229)(+j2.646)}$$

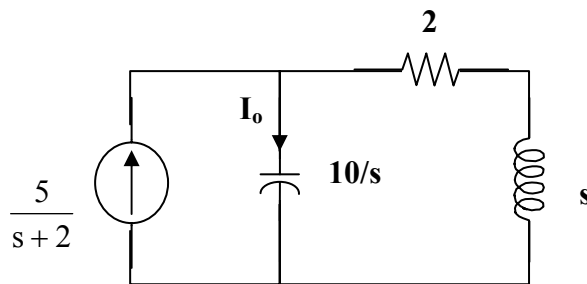
$$= \frac{1}{s+2} + \frac{(1.5 - j1.3229)(-j2.646)}{s+0.5 + j1.3229} + \frac{(1.5 + j1.3229)(+j2.646)}{s+0.5 - j1.3229}$$

$$i_o(t) = \left(e^{-2t} + 0.3779e^{-90^\circ} e^{-t/2} e^{-j1.3229t} + 0.3779e^{90^\circ} e^{-t/2} e^{j1.3229t} \right) u(t) \text{ A}$$

or

$$= \left(e^{-2t} - 0.7559 \sin 1.3229t \right) u(t) \text{ A}$$

Chapter 16, Solution 6.



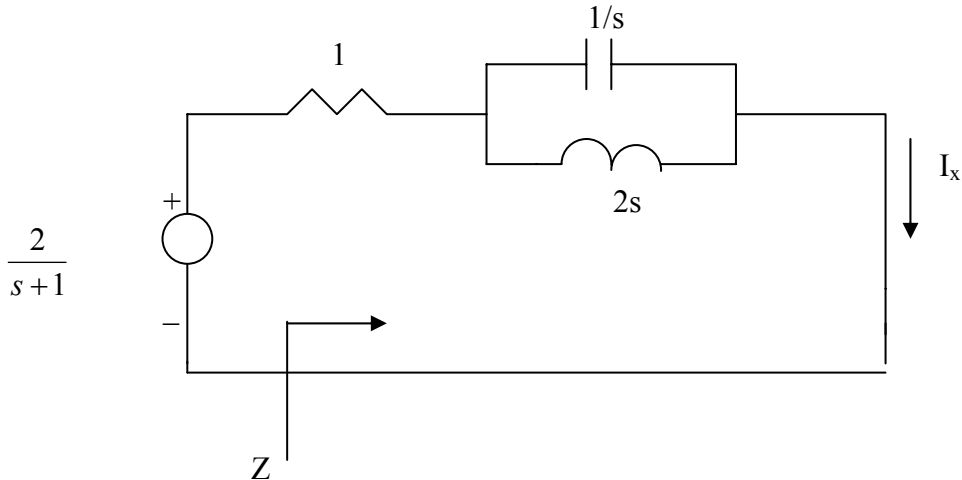
Use current division.

$$I_o = \frac{s+2}{s+2 + \frac{10}{s}} \frac{5}{s+2} = \frac{5s}{s^2 + 2s + 10} = \frac{5(s+1)}{(s+1)^2 + 3^2} - \frac{5}{(s+1)^2 + 3^2}$$

$$i_o(t) = \underline{5e^{-t} \cos 3t - \frac{5}{3} e^{-t} \sin 3t}$$

Chapter 16, Solution 7.

The s-domain version of the circuit is shown below.



$$Z = 1 + \frac{1}{s} // 2s = 1 + \frac{\frac{1}{s}(2s)}{\frac{1}{s} + 2s} = 1 + \frac{2s}{1 + 2s^2} = \frac{2s^2 + 2s + 1}{1 + 2s^2}$$

$$I_x = \frac{V}{Z} = \frac{2}{s+1} \times \frac{1 + 2s^2}{2s^2 + 2s + 1} = \frac{2s^2 + 1}{(s+1)(s^2 + s + 0.5)} = \frac{A}{s+1} + \frac{Bs + C}{s^2 + s + 0.5}$$

$$2s^2 + 1 = A(s^2 + s + 0.5) + B(s^2 + s) + C(s + 1)$$

$$s^2: \quad 2 = A + B$$

$$s: \quad 0 = A + B + C = 2 + C \quad \longrightarrow \quad C = -2$$

$$\text{constant:} \quad 1 = 0.5A + C \text{ or } 0.5A = 3 \quad \longrightarrow \quad A = 6, B = -4$$

$$I_x = \frac{6}{s+1} - \frac{4s+2}{(s+0.5)^2 + 0.75} = \frac{6}{s+1} - \frac{4(s+0.5)}{(s+0.5)^2 + 0.866^2}$$

$$i_x(t) = \underline{\underline{\left[6 - 4e^{-0.5t} \cos 0.866t \right] u(t) \text{ A}}}$$

Chapter 16, Solution 8.

$$(a) \quad Z = \frac{1}{s} + 1 \parallel (1 + 2s) = \frac{1}{s} + \frac{(1 + 2s)}{2 + 2s} = \frac{s^2 + 1.5s + 1}{s(s + 1)}$$

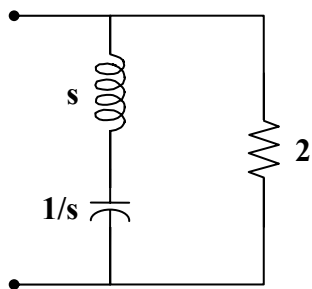
$$(b) \quad \frac{1}{Z} = \frac{1}{2} + \frac{1}{s} + \frac{1}{1 + \frac{1}{s}} = \frac{3s^2 + 3s + 2}{2s(s + 1)}$$

$$Z = \frac{2s(s + 1)}{3s^2 + 3s + 2}$$

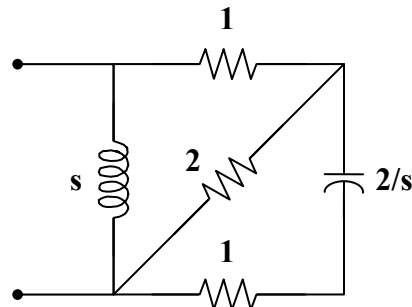
Chapter 16, Solution 9.

(a) The s-domain form of the circuit is shown in Fig. (a).

$$Z_{in} = 2 \parallel (s + 1/s) = \frac{2(s + 1/s)}{2 + s + 1/s} = \frac{2(s^2 + 1)}{s^2 + 2s + 1}$$



(a)



(b)

(b) The s-domain equivalent circuit is shown in Fig. (b).

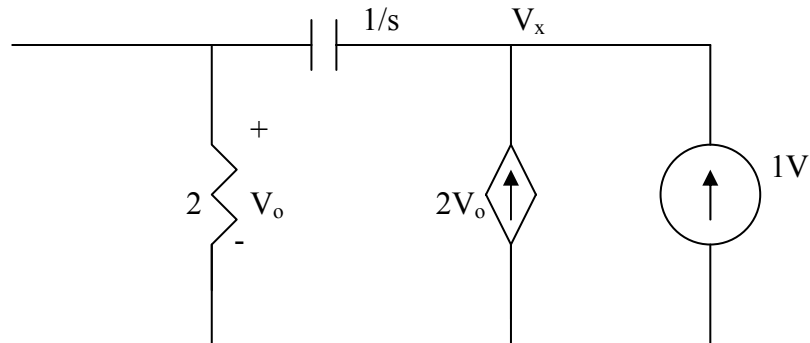
$$2 \parallel (1 + 2/s) = \frac{2(1 + 2/s)}{3 + 2/s} = \frac{2(s + 2)}{3s + 2}$$

$$1 + 2 \parallel (1 + 2/s) = \frac{5s + 6}{3s + 2}$$

$$Z_{in} = s \parallel \left(\frac{5s + 6}{3s + 2} \right) = \frac{s \cdot \left(\frac{5s + 6}{3s + 2} \right)}{s + \left(\frac{5s + 6}{3s + 2} \right)} = \frac{s(5s + 6)}{3s^2 + 7s + 6}$$

Chapter 16, Solution 10.

To find Z_{Th} , consider the circuit below.



Applying KCL gives

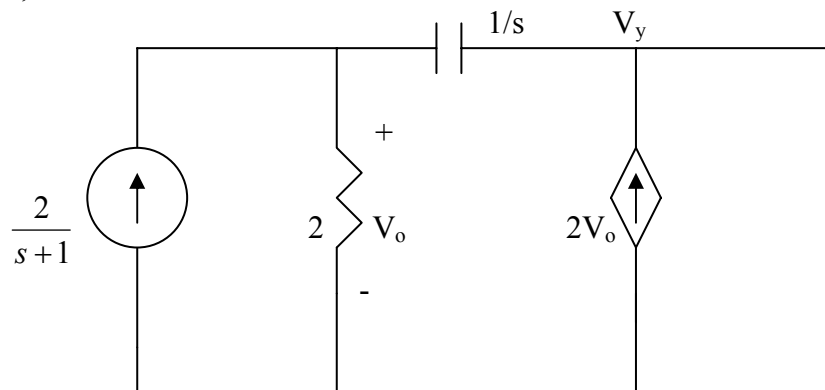
$$1 + 2V_o = \frac{V_x}{2 + 1/s}$$

But $V_o = \frac{2}{2 + 1/s} V_x$. Hence

$$1 + \frac{4V_x}{2 + 1/s} = \frac{V_x}{2 + 1/s} \longrightarrow V_x = -\frac{(2s + 1)}{3s}$$

$$Z_{Th} = \frac{V_x}{1} = -\frac{(2s + 1)}{3s}$$

To find V_{Th} , consider the circuit below.



Applying KCL gives

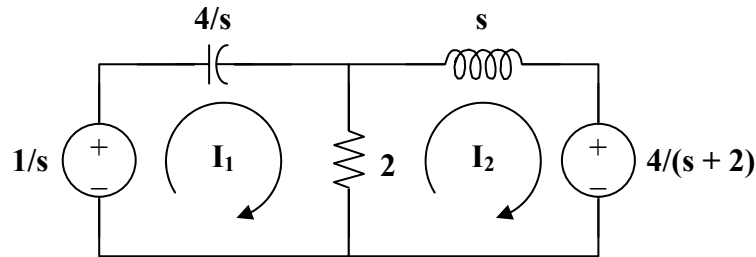
$$\frac{2}{s+1} + 2V_o = \frac{V_o}{2} \longrightarrow V_o = -\frac{4}{3(s+1)}$$

But $-V_y + 2V_o \cdot \frac{1}{s} + V_o = 0$

$$V_{Th} = V_y = V_o \left(1 + \frac{2}{s}\right) = -\frac{4}{3(s+1)} \left(\frac{s+2}{s}\right) = \underline{\underline{\frac{-4(s+2)}{3s(s+1)}}}$$

Chapter 16, Solution 11.

The s-domain form of the circuit is shown below.



Write the mesh equations.

$$\frac{1}{s} = \left(2 + \frac{4}{s}\right) I_1 - 2I_2 \quad (1)$$

$$\frac{-4}{s+2} = -2I_1 + (s+2) I_2 \quad (2)$$

Put equations (1) and (2) into matrix form.

$$\begin{bmatrix} 1/s \\ -4/(s+2) \end{bmatrix} = \begin{bmatrix} 2+4/s & -2 \\ -2 & s+2 \end{bmatrix} \begin{bmatrix} I_1 \\ I_2 \end{bmatrix}$$

$$\Delta = \frac{2}{s}(s^2 + 2s + 4), \quad \Delta_1 = \frac{s^2 - 4s + 4}{s(s+2)}, \quad \Delta_2 = \frac{-6}{s}$$

$$I_1 = \frac{\Delta_1}{\Delta} = \frac{1/2 \cdot (s^2 - 4s + 4)}{(s+2)(s^2 + 2s + 4)} = \frac{A}{s+2} + \frac{Bs+C}{s^2 + 2s + 4}$$

$$1/2 \cdot (s^2 - 4s + 4) = A(s^2 + 2s + 4) + B(s^2 + 2s) + C(s + 2)$$

Equating coefficients :

$$s^2: \quad 1/2 = A + B$$

$$s^1: \quad -2 = 2A + 2B + C$$

$$s^0: \quad 2 = 4A + 2C$$

Solving these equations leads to $A = 2$, $B = -3/2$, $C = -3$

$$I_1 = \frac{2}{s+2} + \frac{-3/2s-3}{(s+1)^2 + (\sqrt{3})^2}$$

$$I_1 = \frac{2}{s+2} + \frac{-3}{2} \cdot \frac{(s+1)}{(s+1)^2 + (\sqrt{3})^2} + \frac{-3}{2\sqrt{3}} \cdot \frac{\sqrt{3}}{(s+1)^2 + (\sqrt{3})^2}$$

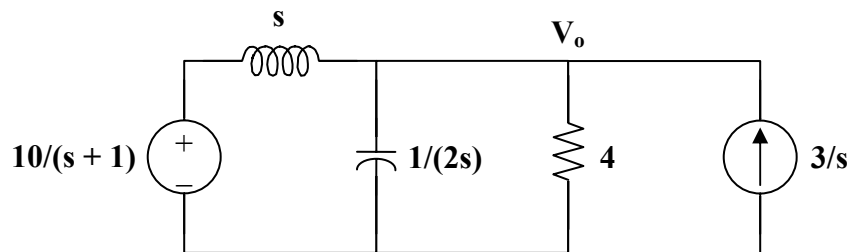
$$i_1(t) = \underline{\underline{[2e^{-2t} - 1.5e^{-t} \cos(1.732t) - 0.866 \sin(1.732t)]u(t) \text{ A}}}$$

$$I_2 = \frac{\Delta_2}{\Delta} = \frac{-6}{s} \cdot \frac{s}{2(s^2 + 2s + 4)} = \frac{-3}{(s+1)^2 + (\sqrt{3})^2}$$

$$i_2(t) = \frac{-3}{\sqrt{3}} e^{-t} \sin(\sqrt{3}t) = \underline{\underline{-1.732 e^{-t} \sin(1.732t)u(t) \text{ A}}}$$

Chapter 16, Solution 12.

We apply nodal analysis to the s-domain form of the circuit below.



$$\frac{10}{s+1} - \frac{V_o}{s} + \frac{3}{s} = \frac{V_o}{4} + 2sV_o$$

$$(1 + 0.25s + s^2)V_o = \frac{10}{s+1} + 15 = \frac{10 + 15s + 15}{s+1}$$

$$V_o = \frac{15s + 25}{(s+1)(s^2 + 0.25s + 1)} = \frac{A}{s+1} + \frac{Bs + C}{s^2 + 0.25s + 1}$$

$$A = (s+1)V_o \Big|_{s=-1} = \frac{40}{7}$$

$$15s + 25 = A(s^2 + 0.25s + 1) + B(s^2 + s) + C(s + 1)$$

Equating coefficients :

$$s^2: \quad 0 = A + B \quad \longrightarrow \quad B = -A$$

$$s^1: \quad 15 = 0.25A + B + C = -0.75A + C$$

$$s^0: \quad 25 = A + C$$

$$A = 40/7, \quad B = -40/7, \quad C = 135/7$$

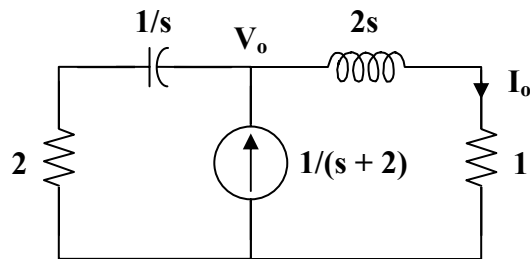
$$V_o = \frac{40}{s+1} + \frac{-40}{\left(s+\frac{1}{2}\right)^2 + \frac{3}{4}} + \frac{135}{7} = \frac{40}{7} \frac{1}{s+1} - \frac{40}{7} \frac{s+\frac{1}{2}}{\left(s+\frac{1}{2}\right)^2 + \frac{3}{4}} + \left(\frac{155}{7} \cdot \frac{2}{\sqrt{3}}\right) \frac{\frac{\sqrt{3}}{2}}{\left(s+\frac{1}{2}\right)^2 + \frac{3}{4}}$$

$$v_o(t) = \frac{40}{7} e^{-t} - \frac{40}{7} e^{-t/2} \cos\left(\frac{\sqrt{3}}{2}t\right) + \frac{(155)(2)}{(7)(\sqrt{3})} e^{-t/2} \sin\left(\frac{\sqrt{3}}{2}t\right)$$

$$v_o(t) = \underline{\underline{5.714 e^{-t} - 5.714 e^{-t/2} \cos(0.866t) + 25.57 e^{-t/2} \sin(0.866t) \text{ V}}}$$

Chapter 16, Solution 13.

Consider the following circuit.



Applying KCL at node o,

$$\frac{1}{s+2} = \frac{V_o}{2s+1} + \frac{V_o}{2+1/s} = \frac{s+1}{2s+1} V_o$$

$$V_o = \frac{2s+1}{(s+1)(s+2)}$$

$$I_o = \frac{V_o}{2s+1} = \frac{1}{(s+1)(s+2)} = \frac{A}{s+1} + \frac{B}{s+2}$$

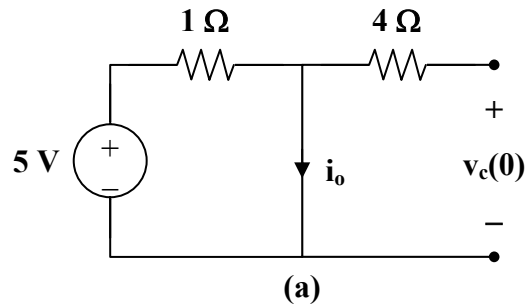
$$A = 1, \quad B = -1$$

$$I_o = \frac{1}{s+1} - \frac{1}{s+2}$$

$$i_o(t) = \underline{(e^{-t} - e^{-2t})u(t) \text{ A}}$$

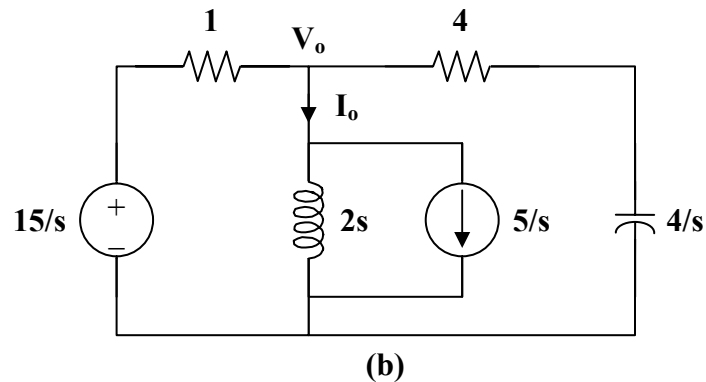
Chapter 16, Solution 14.

We first find the initial conditions from the circuit in Fig. (a).



$$i_o(0^-) = 5 \text{ A}, \quad v_c(0^-) = 0 \text{ V}$$

We now incorporate these conditions in the s-domain circuit as shown in Fig. (b).



At node o,

$$\frac{V_o - 15/s}{1} + \frac{V_o}{2s} + \frac{5}{s} + \frac{V_o - 0}{4 + 4/s} = 0$$

$$\frac{15}{s} - \frac{5}{s} = \left(1 + \frac{1}{2s} + \frac{s}{4(s+1)}\right) V_o$$

$$\frac{10}{s} = \frac{4s^2 + 4s + 2s + 2 + s^2}{4s(s+1)} V_o = \frac{5s^2 + 6s + 2}{4s(s+1)} V_o$$

$$V_o = \frac{40(s+1)}{5s^2 + 6s + 2}$$

$$I_o = \frac{V_o}{2s} + \frac{5}{s} = \frac{4(s+1)}{s(s^2 + 1.2s + 0.4)} + \frac{5}{s}$$

$$I_o = \frac{5}{s} + \frac{A}{s} + \frac{Bs + C}{s^2 + 1.2s + 0.4}$$

$$4(s+1) = A(s^2 + 1.2s + 0.4) + Bs^s + Cs$$

Equating coefficients :

$$s^0: \quad 4 = 0.4A \quad \longrightarrow \quad A = 10$$

$$s^1: \quad 4 = 1.2A + C \quad \longrightarrow \quad C = -1.2A + 4 = -8$$

$$s^2: \quad 0 = A + B \quad \longrightarrow \quad B = -A = -10$$

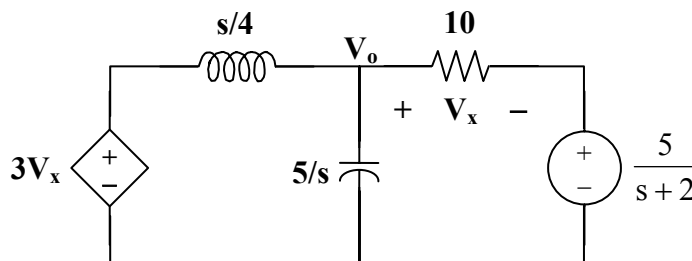
$$I_o = \frac{5}{s} + \frac{10}{s} - \frac{10s + 8}{s^2 + 1.2s + 0.4}$$

$$I_o = \frac{15}{s} - \frac{10(s+0.6)}{(s+0.6)^2 + 0.2^2} - \frac{10(0.2)}{(s+0.6)^2 + 0.2^2}$$

$$i_o(t) = \underline{\underline{[15 - 10e^{-0.6t}(\cos(0.2t) - \sin(0.2t))] u(t) \text{ A}}}$$

Chapter 16, Solution 15.

First we need to transform the circuit into the s-domain.



$$\frac{V_o - 3V_x}{s/4} + \frac{V_o - 0}{5/s} + \frac{V_o - \frac{5}{s+2}}{10} = 0$$

$$40V_o - 120V_x + 2s^2V_o + sV_o - \frac{5s}{s+2} = 0 = (2s^2 + s + 40)V_o - 120V_x - \frac{5s}{s+2}$$

$$\text{But, } V_x = V_o - \frac{5}{s+2} \rightarrow V_o = V_x + \frac{5}{s+2}$$

We can now solve for V_x .

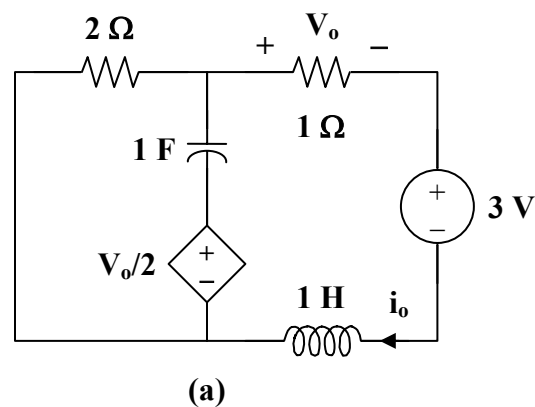
$$(2s^2 + s + 40)\left(V_x + \frac{5}{s+2}\right) - 120V_x - \frac{5s}{s+2} = 0$$

$$2(s^2 + 0.5s - 40)V_x = -10\frac{(s^2 + 20)}{s+2}$$

$$V_x = -5\frac{(s^2 + 20)}{(s+2)(s^2 + 0.5s - 40)}$$

Chapter 16, Solution 16.

We first need to find the initial conditions. For $t < 0$, the circuit is shown in Fig. (a). To dc, the capacitor acts like an open circuit and the inductor acts like a short circuit.

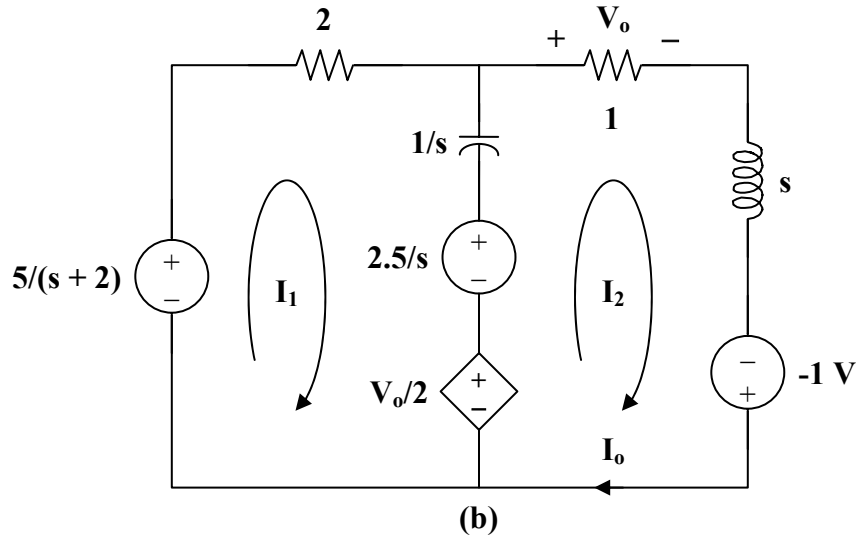


Hence,

$$i_L(0) = i_o = \frac{-3}{3} = -1 \text{ A}, \quad v_o = -1 \text{ V}$$

$$v_c(0) = -(2)(-1) - \left(\frac{-1}{2}\right) = 2.5 \text{ V}$$

We now incorporate the initial conditions for $t > 0$ as shown in Fig. (b).



For mesh 1,

$$\frac{-5}{s+2} + \left(2 + \frac{1}{s}\right)I_1 - \frac{1}{s}I_2 + \frac{2.5}{s} + \frac{V_o}{2} = 0$$

But, $V_o = I_o = I_2$

$$\left(2 + \frac{1}{s}\right)I_1 + \left(\frac{1}{2} - \frac{1}{s}\right)I_2 = \frac{5}{s+2} - \frac{2.5}{s} \quad (1)$$

For mesh 2,

$$\left(1 + s + \frac{1}{s}\right)I_2 - \frac{1}{s}I_1 + 1 - \frac{V_o}{2} - \frac{2.5}{s} = 0$$

$$-\frac{1}{s}I_1 + \left(\frac{1}{2} + s + \frac{1}{s}\right)I_2 = \frac{2.5}{s} - 1 \quad (2)$$

Put (1) and (2) in matrix form.

$$\begin{bmatrix} 2 + \frac{1}{s} & \frac{1}{2} - \frac{1}{s} \\ -\frac{1}{s} & \frac{1}{2} + s + \frac{1}{s} \end{bmatrix} \begin{bmatrix} I_1 \\ I_2 \end{bmatrix} = \begin{bmatrix} \frac{5}{s+2} - \frac{2.5}{s} \\ \frac{2.5}{s} - 1 \end{bmatrix}$$

$$\Delta = 2s + 2 + \frac{3}{s}, \quad \Delta_2 = -2 + \frac{4}{s} + \frac{5}{s(s+2)}$$

$$I_o = I_2 = \frac{\Delta_2}{\Delta} = \frac{-2s^2 + 13}{(s+2)(2s^2 + 2s + 3)} = \frac{A}{s+2} + \frac{Bs+C}{2s^2 + 2s + 3}$$

$$-2s^2 + 13 = A(2s^2 + 2s + 3) + B(s^2 + 2s) + C(s + 2)$$

Equating coefficients :

$$s^2: \quad -2 = 2A + B$$

$$s^1: \quad 0 = 2A + 2B + C$$

$$s^0: \quad 13 = 3A + 2C$$

Solving these equations leads to

$$A = 0.7143, \quad B = -3.429, \quad C = 5.429$$

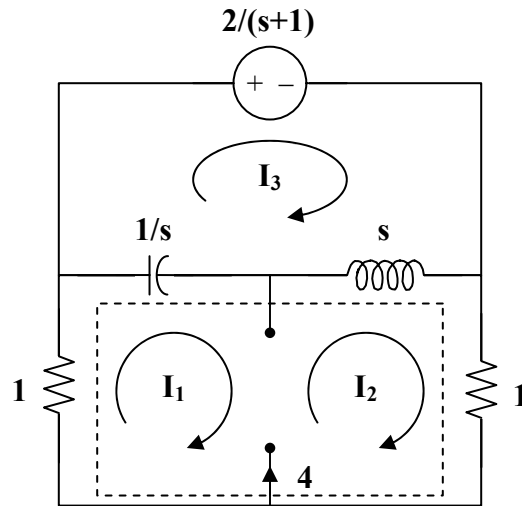
$$I_o = \frac{0.7143}{s+2} - \frac{3.429s - 5.429}{2s^2 + 2s + 3} = \frac{0.7143}{s+2} - \frac{1.7145s - 2.714}{s^2 + s + 1.5}$$

$$I_o = \frac{0.7143}{s+2} - \frac{1.7145(s+0.5)}{(s+0.5)^2 + 1.25} + \frac{(3.194)(\sqrt{1.25})}{(s+0.5)^2 + 1.25}$$

$$i_o(t) = \underline{\underline{[0.7143e^{-2t} - 1.7145e^{-0.5t} \cos(1.25t) + 3.194e^{-0.5t} \sin(1.25t)]u(t) \text{ A}}}$$

Chapter 16, Solution 17.

We apply mesh analysis to the s-domain form of the circuit as shown below.



For mesh 3,

$$\frac{2}{s+1} + \left(s + \frac{1}{s}\right)I_3 - \frac{1}{s}I_1 - sI_2 = 0 \quad (1)$$

For the supermesh,

$$\left(1 + \frac{1}{s}\right)I_1 + (1+s)I_2 - \left(\frac{1}{s} + s\right)I_3 = 0 \quad (2)$$

$$\text{But } I_1 = I_2 - 4 \quad (3)$$

Substituting (3) into (1) and (2) leads to

$$\left(2 + s + \frac{1}{s}\right)I_2 - \left(s + \frac{1}{s}\right)I_3 = 4\left(1 + \frac{1}{s}\right) \quad (4)$$

$$-\left(s + \frac{1}{s}\right)I_2 + \left(s + \frac{1}{s}\right)I_3 = \frac{-4}{s} - \frac{2}{s+1} \quad (5)$$

Adding (4) and (5) gives

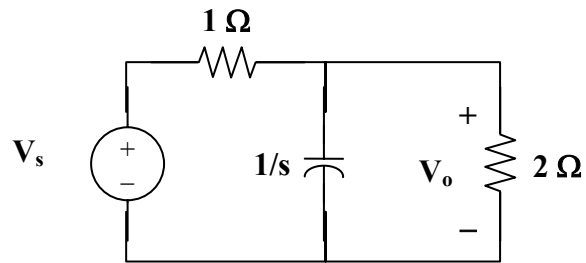
$$2I_2 = 4 - \frac{2}{s+1}$$

$$I_2 = 2 - \frac{1}{s+1}$$

$$i_o(t) = i_2(t) = \underline{(2 - e^{-t})u(t) \text{ A}}$$

Chapter 16, Solution 18.

$$v_s(t) = 3u(t) - 3u(t-1) \text{ or } V_s = \frac{3}{s} - \frac{e^{-s}}{s} = \frac{3}{s}(1 - e^{-s})$$



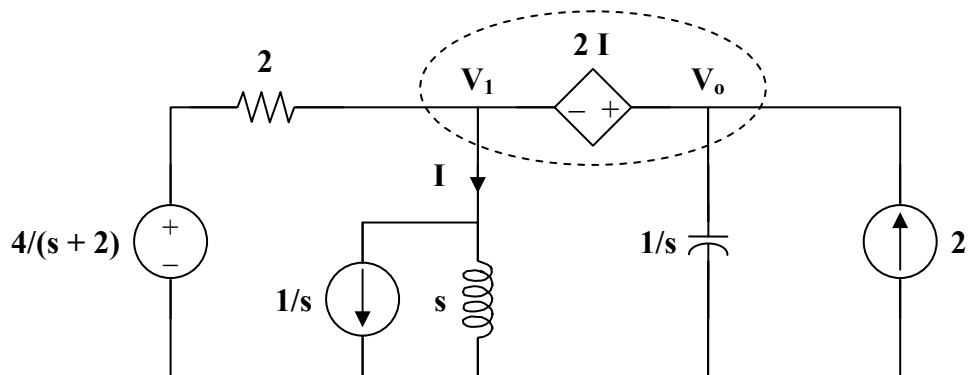
$$\frac{V_o - V_s}{1} + sV_o + \frac{V_o}{2} = 0 \rightarrow (s + 1.5)V_o = V_s$$

$$V_o = \frac{3}{s(s + 1.5)}(1 - e^{-s}) = \left(\frac{2}{s} - \frac{2}{s + 1.5}\right)(1 - e^{-s})$$

$$v_o(t) = \underline{[(2 - 2e^{-1.5t})u(t) - (2 - 2e^{-1.5(t-1)})u(t-1)]V}$$

Chapter 16, Solution 19.

We incorporate the initial conditions in the s-domain circuit as shown below.



At the supernode,

$$\frac{4/(s+2) - V_1}{2} + 2 = \frac{V_1}{s} + \frac{1}{s} + sV_o$$

$$\frac{2}{s+2} + 2 = \left(\frac{1}{2} + \frac{1}{s}\right)V_1 + \frac{1}{s} + sV_o \quad (1)$$

But $V_o = V_1 + 2I$ and $I = \frac{V_1 + 1}{s}$

$$V_o = V_1 + \frac{2(V_1 + 1)}{s} \longrightarrow V_1 = \frac{V_o - 2/s}{(s+2)/s} = \frac{sV_o - 2}{s+2} \quad (2)$$

Substituting (2) into (1)

$$\frac{2}{s+2} + 2 - \frac{1}{s} = \left(\frac{2s+1}{s}\right) \left[\left(\frac{s}{s+2}\right)V_o - \frac{2}{s+2}\right] + sV_o$$

$$\frac{2}{s+2} + 2 - \frac{1}{s} + \frac{2(2s+1)}{s(s+2)} = \left[\left(\frac{2s+1}{s+2}\right) + s\right]V_o$$

$$\frac{2s^2 + 9s}{s(s+2)} = \frac{2s+9}{s+2} = \frac{s^2 + 4s + 1}{s+2} V_o$$

$$V_o = \frac{2s+9}{s^2 + 4s + 1} = \frac{A}{s+0.2679} + \frac{B}{s+3.732}$$

$$A = 2.443, \quad B = -0.4434$$

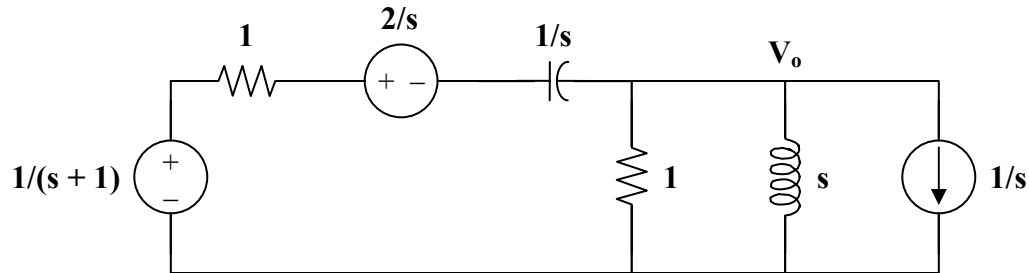
$$V_o = \frac{2.443}{s+0.2679} - \frac{0.4434}{s+3.732}$$

Therefore,

$$v_o(t) = \underline{\underline{(2.443e^{-0.2679t} - 0.4434e^{-3.732t})u(t) \text{ V}}}$$

Chapter 16, Solution 20.

We incorporate the initial conditions and transform the current source to a voltage source as shown.



At the main non-reference node, KCL gives

$$\frac{1/(s+1) - 2/s - V_o}{1 + 1/s} = \frac{V_o}{1} + \frac{V_o}{s} + \frac{1}{s}$$

$$\frac{s}{s+1} - 2 - sV_o = (s+1)(s+1/s)V_o + \frac{s+1}{s}$$

$$\frac{s}{s+1} - \frac{s+1}{s} - 2 = (2s + 2 + 1/s)V_o$$

$$V_o = \frac{-2s^2 - 4s - 1}{(s+1)(2s^2 + 2s + 1)}$$

$$V_o = \frac{-s - 2s - 0.5}{(s+1)(s^2 + s + 0.5)} = \frac{A}{s+1} + \frac{Bs + C}{s^2 + s + 0.5}$$

$$A = (s+1)V_o \Big|_{s=-1} = 1$$

$$-s^2 - 2s - 0.5 = A(s^2 + s + 0.5) + B(s^2 + s) + C(s+1)$$

Equating coefficients :

$$s^2: \quad -1 = A + B \quad \longrightarrow \quad B = -2$$

$$s^1: \quad -2 = A + B + C \quad \longrightarrow \quad C = -1$$

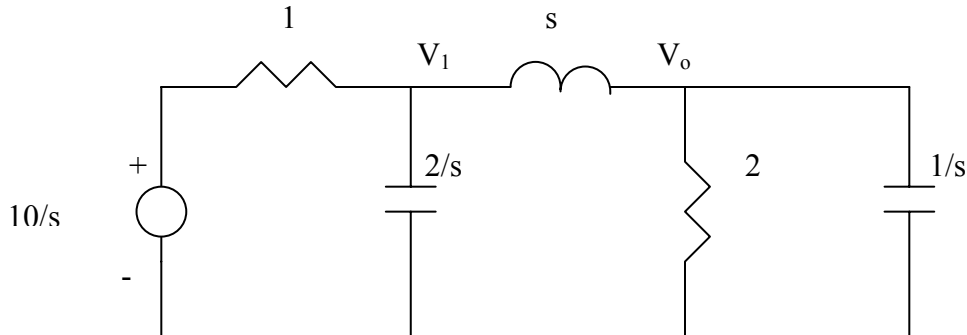
$$s^0: \quad -0.5 = 0.5A + C = 0.5 - 1 = -0.5$$

$$V_o = \frac{1}{s+1} - \frac{2s+1}{s^2 + s + 0.5} = \frac{1}{s+1} - \frac{2(s+0.5)}{(s+0.5)^2 + (0.5)^2}$$

$$v_o(t) = \underline{\underline{[e^{-t} - 2e^{-t/2} \cos(t/2)]u(t) \text{ V}}}$$

Chapter 16, Solution 21.

The s-domain version of the circuit is shown below.



At node 1,

$$\frac{10}{s} - V_1 = \frac{V_1 - V_o}{s} + \frac{s}{2} V_o \quad \longrightarrow \quad 10 = (s+1)V_1 + \left(\frac{s^2}{2} - 1\right)V_o \quad (1)$$

At node 2,

$$\frac{V_1 - V_o}{s} = \frac{V_o}{2} + sV_o \quad \longrightarrow \quad V_1 = V_o \left(\frac{s}{2} + s^2 + 1\right) \quad (2)$$

Substituting (2) into (1) gives

$$10 = (s+1)(s^2 + s/2 + 1)V_o + \left(\frac{s^2}{2} - 1\right)V_o = s(s^2 + 2s + 1.5)V_o$$

$$V_o = \frac{10}{s(s^2 + 2s + 1.5)} = \frac{A}{s} + \frac{Bs + C}{s^2 + 2s + 1.5}$$

$$10 = A(s^2 + 2s + 1.5) + Bs^2 + Cs$$

$$s^2 : \quad 0 = A + B$$

$$s : \quad 0 = 2A + C$$

$$\text{constant :} \quad 10 = 1.5A \quad \longrightarrow \quad A = 20/3, B = -20/3, C = -40/3$$

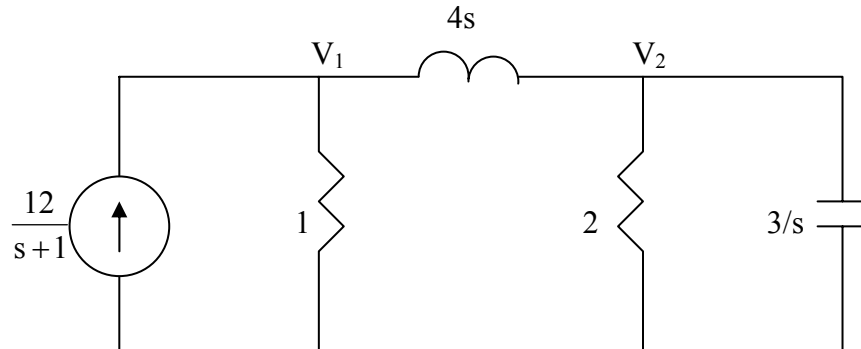
$$V_o = \frac{20}{3} \left[\frac{1}{s} - \frac{s+2}{s^2 + 2s + 1.5} \right] = \frac{20}{3} \left[\frac{1}{s} - \frac{s+1}{(s+1)^2 + 0.7071^2} - 1.414 \frac{0.7071}{(s+1)^2 + 0.7071^2} \right]$$

Taking the inverse Laplace transform finally yields

$$v_o(t) = \frac{20}{3} \left[1 - e^{-t} \cos 0.7071t - 1.414 e^{-t} \sin 0.7071t \right] u(t) \text{ V}$$

Chapter 16, Solution 22.

The s-domain version of the circuit is shown below.



At node 1,

$$\frac{12}{s+1} = \frac{V_1}{1} + \frac{V_1 - V_2}{4s} \longrightarrow \frac{12}{s+1} = V_1 \left(1 + \frac{1}{4s} \right) - \frac{V_2}{4s} \quad (1)$$

At node 2,

$$\frac{V_1 - V_2}{4s} = \frac{V_2}{2} + \frac{s}{3} V_2 \longrightarrow V_1 = V_2 \left(\frac{4}{3} s^2 + 2s + 1 \right) \quad (2)$$

Substituting (2) into (1),

$$\frac{12}{s+1} = V_2 \left[\left(\frac{4}{3} s^2 + 2s + 1 \right) \left(1 + \frac{1}{4s} \right) - \frac{1}{4s} \right] = \left(\frac{4}{3} s^2 + \frac{7}{3} s + \frac{3}{2} \right) V_2$$

$$V_2 = \frac{9}{(s+1) \left(s^2 + \frac{7}{4} s + \frac{9}{8} \right)} = \frac{A}{(s+1)} + \frac{Bs+C}{\left(s^2 + \frac{7}{4} s + \frac{9}{8} \right)}$$

$$9 = A \left(s^2 + \frac{7}{4} s + \frac{9}{8} \right) + B(s^2 + s) + C(s+1)$$

Equating coefficients:

$$s^2 : \quad 0 = A + B$$

$$s : \quad 0 = \frac{7}{4} A + B + C = \frac{3}{4} A + C \longrightarrow C = -\frac{3}{4} A$$

$$\text{constant :} \quad 9 = \frac{9}{8} A + C = \frac{3}{8} A \longrightarrow A = 24, B = -24, C = -18$$

$$V_2 = \frac{24}{(s+1)} - \frac{24s+18}{(s^2 + \frac{7}{4}s + \frac{9}{8})} = \frac{24}{(s+1)} - \frac{24(s+7/8)}{(s+\frac{7}{8})^2 + \frac{23}{64}} + \frac{3}{(s+\frac{7}{8})^2 + \frac{23}{64}}$$

Taking the inverse of this produces:

$$v_2(t) = \underline{\left[24e^{-t} - 24e^{-0.875t} \cos(0.5995t) + 5.004e^{-0.875t} \sin(0.5995t) \right] u(t)}$$

Similarly,

$$V_1 = \frac{9\left(\frac{4}{3}s^2 + 2s + 1\right)}{(s+1)(s^2 + \frac{7}{4}s + \frac{9}{8})} = \frac{D}{(s+1)} + \frac{Es + F}{(s^2 + \frac{7}{4}s + \frac{9}{8})}$$

$$9\left(\frac{4}{3}s^2 + 2s + 1\right) = D\left(s^2 + \frac{7}{4}s + \frac{9}{8}\right) + E(s^2 + s) + F(s+1)$$

Equating coefficients:

$$s^2 : \quad 12 = D + E$$

$$s : \quad 18 = \frac{7}{4}D + E + F \text{ or } 6 = \frac{3}{4}D + F \quad \longrightarrow \quad F = 6 - \frac{3}{4}D$$

$$\text{constant :} \quad 9 = \frac{9}{8}D + F \text{ or } 3 = \frac{3}{8}D \quad \longrightarrow \quad D = 8, E = 4, F = 0$$

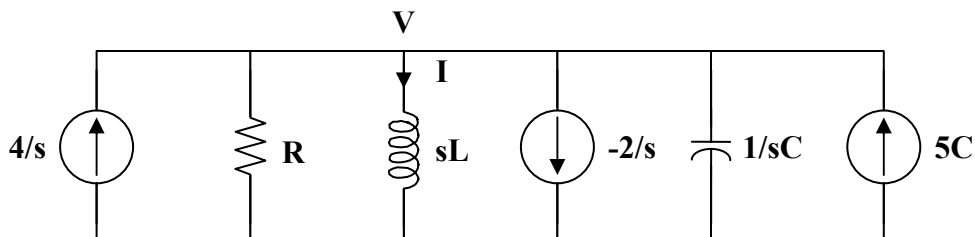
$$V_1 = \frac{8}{(s+1)} + \frac{4s}{(s^2 + \frac{7}{4}s + \frac{9}{8})} = \frac{8}{(s+1)} + \frac{4(s+7/8)}{(s+\frac{7}{8})^2 + \frac{23}{64}} - \frac{7/2}{(s+\frac{7}{8})^2 + \frac{23}{64}}$$

Thus,

$$v_1(t) = \underline{\left[8e^{-t} + 4e^{-0.875t} \cos(0.5995t) - 5.838e^{-0.875t} \sin(0.5995t) \right] u(t)}$$

Chapter 16, Solution 23.

The s-domain form of the circuit with the initial conditions is shown below.



At the non-reference node,

$$\frac{4}{s} + \frac{2}{s} + 5C = \frac{V}{R} + \frac{V}{sL} + sCV$$

$$\frac{6 + 5sC}{s} = \frac{CV}{s} \left(s^2 + \frac{s}{RC} + \frac{1}{LC} \right)$$

$$V = \frac{5s + 6/C}{s^2 + s/RC + 1/LC}$$

But $\frac{1}{RC} = \frac{1}{10/80} = 8$, $\frac{1}{LC} = \frac{1}{4/80} = 20$

$$V = \frac{5s + 480}{s^2 + 8s + 20} = \frac{5(s + 4)}{(s + 4)^2 + 2^2} + \frac{(230)(2)}{(s + 4)^2 + 2^2}$$

$$v(t) = \underline{\underline{5e^{-4t} \cos(2t) + 230e^{-4t} \sin(2t) \text{ V}}}$$

$$I = \frac{V}{sL} = \frac{5s + 480}{4s(s^2 + 8s + 20)}$$

$$I = \frac{1.25s + 120}{s(s^2 + 8s + 20)} = \frac{A}{s} + \frac{Bs + C}{s^2 + 8s + 20}$$

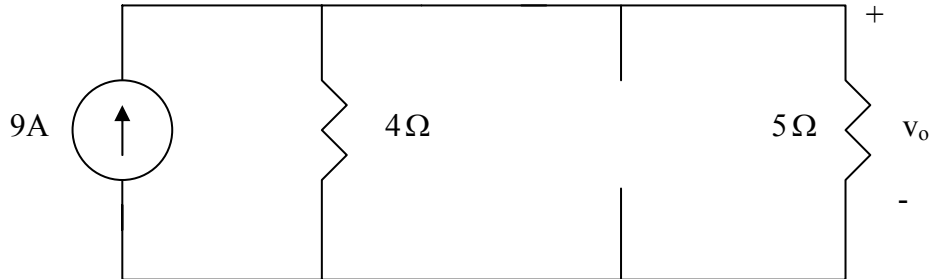
$$A = 6, \quad B = -6, \quad C = -46.75$$

$$I = \frac{6}{s} - \frac{6s + 46.75}{s^2 + 8s + 20} = \frac{6}{s} - \frac{6(s + 4)}{(s + 4)^2 + 2^2} - \frac{(11.375)(2)}{(s + 4)^2 + 2^2}$$

$$i(t) = \underline{\underline{6u(t) - 6e^{-4t} \cos(2t) - 11.375e^{-4t} \sin(2t), \quad t > 0}}$$

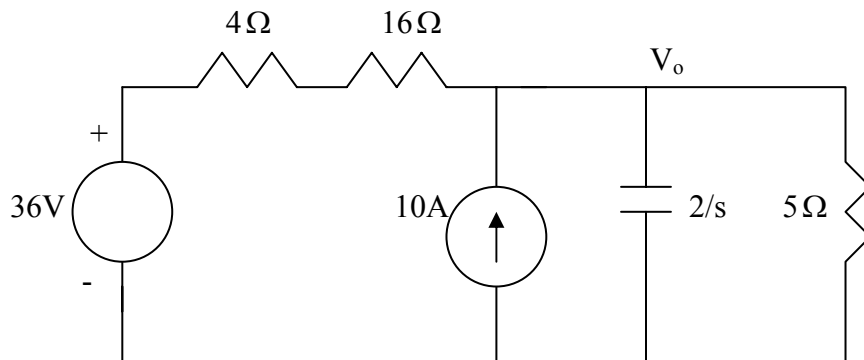
Chapter 16, Solution 24.

At $t = 0^-$, the circuit is equivalent to that shown below.



$$v_o(0) = 5 \times \frac{4}{4+5} (9) = 20$$

For $t > 0$, we have the Laplace transform of the circuit as shown below after transforming the current source to a voltage source.



Applying KCL gives

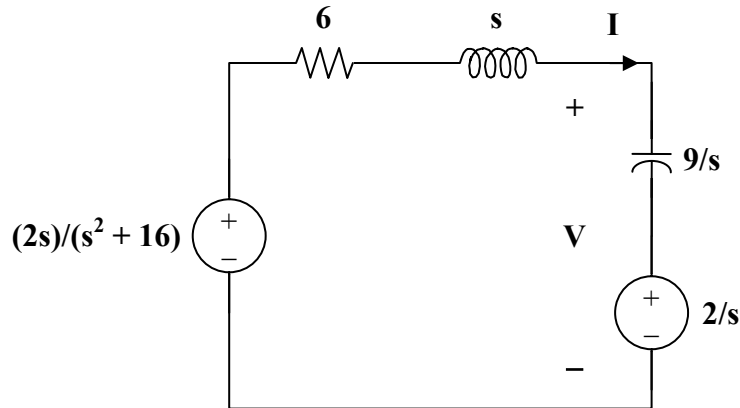
$$\frac{36 - V_o}{20} + 10 = \frac{sV_o}{2} + \frac{V_o}{5} \quad \longrightarrow \quad V_o = \frac{3.6 + 20s}{s(s+0.5)} = \frac{A}{s} + \frac{B}{s+0.5}, \quad A = 7.2, B = -12.8$$

Thus,

$$v_o(t) = \underline{\underline{[7.2 - 12.8e^{-0.5t}]} u(t)}$$

Chapter 16, Solution 25.

For $t > 0$, the circuit in the s-domain is shown below.



Applying KVL,

$$\frac{-2s}{s^2 + 16} + \left(6 + s + \frac{9}{s}\right)I + \frac{2}{s} = 0$$

$$I = \frac{4s^2 + 32}{(s^2 + 6s + 9)(s^2 + 16)}$$

$$V = \frac{9}{s}I + \frac{2}{s} = \frac{2}{s} + \frac{36s^2 + 288}{s(s+3)^2(s^2 + 16)}$$

$$= \frac{2}{s} + \frac{A}{s} + \frac{B}{s+3} + \frac{C}{(s+3)^2} + \frac{Ds + E}{s^2 + 16}$$

$$36s^2 + 288 = A(s^4 + 6s^3 + 25s^2 + 96s + 144) + B(s^4 + 3s^3 + 16s^2 + 48s) \\ + C(s^3 + 16s) + D(s^4 + 6s^3 + 9s^2) + E(s^3 + 6s^2 + 9s)$$

Equating coefficients :

$$s^0: \quad 288 = 144A \quad (1)$$

$$s^1: \quad 0 = 96A + 48B + 16C + 9E \quad (2)$$

$$s^2: \quad 36 = 25A + 16B + 9D + 6E \quad (3)$$

$$s^3: \quad 0 = 6A + 3B + C + 6D + E \quad (4)$$

$$s^4: \quad 0 = A + B + D \quad (5)$$

Solving equations (1), (2), (3), (4) and (5) gives

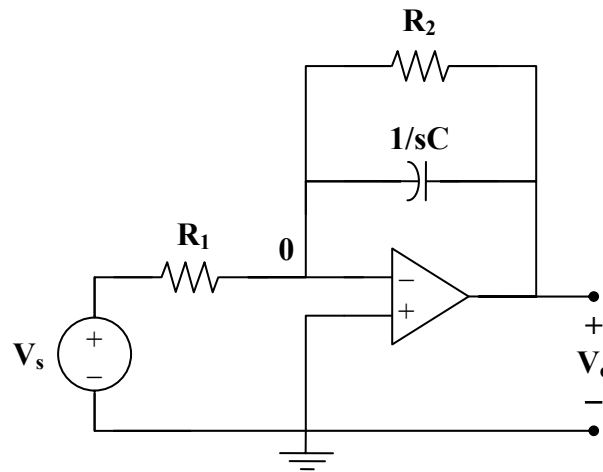
$$A = 2, \quad B = -1.7984, \quad C = -8.16, \quad D = -0.2016, \quad E = 2.765$$

$$V(s) = \frac{4}{s} - \frac{1.7984}{s+3} - \frac{8.16}{(s+3)^2} - \frac{0.2016s}{s^2+16} + \frac{(0.6912)(4)}{s^2+16}$$

$$v(t) = \underline{4u(t) - 1.7984e^{-3t} - 8.16te^{-3t} - 0.2016\cos(4t) + 0.6912\sin(4t) \text{ V}}$$

Chapter 16, Solution 26.

Consider the op-amp circuit below.



At node 0,

$$\frac{V_s - 0}{R_1} = \frac{0 - V_o}{R_2} + (0 - V_o)sC$$

$$V_s = R_1 \left(\frac{1}{R_2} + sC \right) (-V_o)$$

$$\frac{V_o}{V_s} = \frac{-1}{sR_1C + R_1/R_2}$$

But $\frac{R_1}{R_2} = \frac{20}{10} = 2$, $R_1C = (20 \times 10^3)(50 \times 10^{-6}) = 1$

So, $\frac{V_o}{V_s} = \frac{-1}{s+2}$

$$V_s = 3e^{-5t} \longrightarrow V_s = 3/(s+5)$$

$$V_o = \frac{-3}{(s+2)(s+5)}$$

$$-V_o = \frac{3}{(s+2)(s+5)} = \frac{A}{s+2} + \frac{B}{s+5}$$

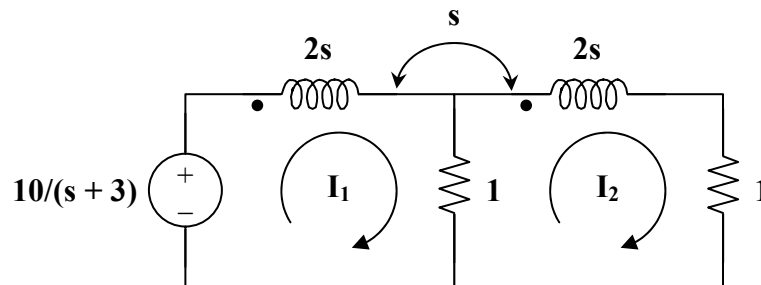
$$A=1, \quad B=-1$$

$$V_o = \frac{1}{s+5} - \frac{1}{s+2}$$

$$v_o(t) = \underline{(e^{-5t} - e^{-2t})u(t)}$$

Chapter 16, Solution 27.

Consider the following circuit.



For mesh 1,

$$\frac{10}{s+3} = (1+2s)I_1 - I_2 - sI_2$$

$$\frac{10}{s+3} = (1+2s)I_1 - (1+s)I_2 \quad (1)$$

For mesh 2,

$$0 = (2+2s)I_2 - I_1 - sI_1$$

$$0 = -(1+s)I_1 + 2(s+1)I_2 \quad (2)$$

(1) and (2) in matrix form,

$$\begin{bmatrix} 10/(s+3) \\ 0 \end{bmatrix} = \begin{bmatrix} 2s+1 & -(s+1) \\ -(s+1) & 2(s+1) \end{bmatrix} \begin{bmatrix} I_1 \\ I_2 \end{bmatrix}$$

$$\Delta = 3s^2 + 4s + 1$$

$$\Delta_1 = \frac{20(s+1)}{s+3}$$

$$\Delta_2 = \frac{10(s+1)}{s+3}$$

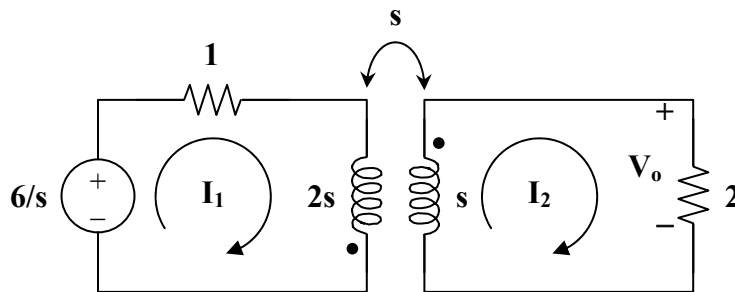
Thus

$$I_1 = \frac{\Delta_1}{\Delta} = \frac{20(s+1)}{(s+3)(3s^2+4s+1)}$$

$$I_2 = \frac{\Delta_2}{\Delta} = \frac{10(s+1)}{(s+3)(3s^2+4s+1)} = \frac{I_1}{2}$$

Chapter 16, Solution 28.

Consider the circuit shown below.



For mesh 1,

$$\frac{6}{s} = (1+2s)I_1 + sI_2 \quad (1)$$

For mesh 2,

$$0 = sI_1 + (2+s)I_2$$

$$I_1 = -\left(1 + \frac{2}{s}\right)I_2 \quad (2)$$

Substituting (2) into (1) gives

$$\frac{6}{s} = -(1+2s)\left(1 + \frac{2}{s}\right)I_2 + sI_2 = \frac{-(s^2+5s+2)}{s}I_2$$

or
$$I_2 = \frac{-6}{s^2+5s+2}$$

$$V_o = 2I_2 = \frac{-12}{s^2 + 5s + 2} = \frac{-12}{(s + 0.438)(s + 4.561)}$$

Since the roots of $s^2 + 5s + 2 = 0$ are -0.438 and -4.561,

$$V_o = \frac{A}{s + 0.438} + \frac{B}{s + 4.561}$$

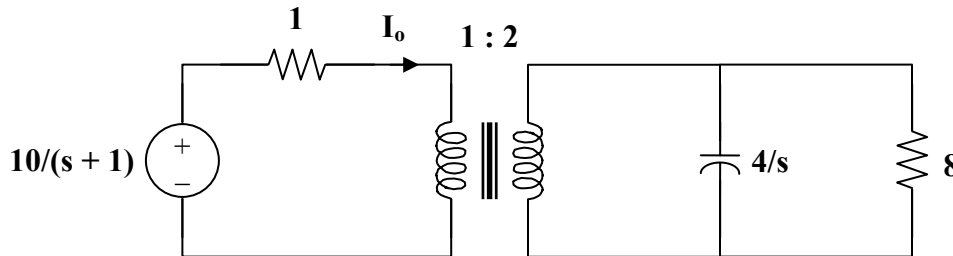
$$A = \frac{-12}{4.123} = -2.91, \quad B = \frac{-12}{-4.123} = 2.91$$

$$V_o(s) = \frac{-2.91}{s + 0.438} + \frac{2.91}{s + 4.561}$$

$$v_o(t) = \underline{2.91[e^{-4.561t} - e^{0.438t}]} u(t) \text{ V}$$

Chapter 16, Solution 29.

Consider the following circuit.



$$\text{Let } Z_L = 8 \parallel \frac{4}{s} = \frac{(8)(4/s)}{8 + 4/s} = \frac{8}{2s + 1}$$

When this is reflected to the primary side,

$$Z_{in} = 1 + \frac{Z_L}{n^2}, \quad n = 2$$

$$Z_{in} = 1 + \frac{2}{2s + 1} = \frac{2s + 3}{2s + 1}$$

$$I_o = \frac{10}{s + 1} \cdot \frac{1}{Z_{in}} = \frac{10}{s + 1} \cdot \frac{2s + 1}{2s + 3}$$

$$I_o = \frac{10s+5}{(s+1)(s+1.5)} = \frac{A}{s+1} + \frac{B}{s+1.5}$$

$$A = -10, \quad B = 20$$

$$I_o(s) = \frac{-10}{s+1} + \frac{20}{s+1.5}$$

$$i_o(t) = \underline{\underline{10[2e^{-1.5t} - e^{-t}]\mathbf{u}(t) \text{ A}}}$$

Chapter 16, Solution 30.

$$Y(s) = H(s)X(s), \quad X(s) = \frac{4}{s+1/3} = \frac{12}{3s+1}$$

$$Y(s) = \frac{12s^2}{(3s+1)^2} = \frac{4}{3} - \frac{8s+4/3}{(3s+1)^2}$$

$$Y(s) = \frac{4}{3} - \frac{8}{9} \cdot \frac{s}{(s+1/3)^2} - \frac{4}{27} \cdot \frac{1}{(s+1/3)^2}$$

$$\text{Let } G(s) = \frac{-8}{9} \cdot \frac{s}{(s+1/3)^2}$$

Using the time differentiation property,

$$g(t) = \frac{-8}{9} \cdot \frac{d}{dt}(te^{-t/3}) = \frac{-8}{9} \left(\frac{-1}{3} te^{-t/3} + e^{-t/3} \right)$$

$$g(t) = \frac{8}{27} te^{-t/3} - \frac{8}{9} e^{-t/3}$$

Hence,

$$y(t) = \frac{4}{3} \mathbf{u}(t) + \frac{8}{27} te^{-t/3} - \frac{8}{9} e^{-t/3} - \frac{4}{27} te^{-t/3}$$

$$y(t) = \underline{\underline{\frac{4}{3} \mathbf{u}(t) - \frac{8}{9} e^{-t/3} + \frac{4}{27} te^{-t/3}}}$$

Chapter 16, Solution 31.

$$x(t) = u(t) \longrightarrow X(s) = \frac{1}{s}$$

$$y(t) = 10 \cos(2t) \longrightarrow Y(s) = \frac{10s}{s^2 + 4}$$

$$H(s) = \frac{Y(s)}{X(s)} = \frac{10s^2}{\underline{s^2 + 4}}$$

Chapter 16, Solution 32.

(a) $Y(s) = H(s)X(s)$

$$= \frac{s+3}{s^2+4s+5} \cdot \frac{1}{s}$$

$$= \frac{s+3}{s(s^2+4s+5)} = \frac{A}{s} + \frac{Bs+C}{s^2+4s+5}$$

$$s+3 = A(s^2+4s+5) + Bs^2 + Cs$$

Equating coefficients :

$$s^0: \quad 3 = 5A \longrightarrow A = 3/5$$

$$s^1: \quad 1 = 4A + C \longrightarrow C = 1 - 4A = -7/5$$

$$s^2: \quad 0 = A + B \longrightarrow B = -A = -3/5$$

$$Y(s) = \frac{3/5}{s} - \frac{1}{5} \cdot \frac{3s+7}{s^2+4s+5}$$

$$Y(s) = \frac{0.6}{s} - \frac{1}{5} \cdot \frac{3(s+2)+1}{(s+2)^2+1}$$

$$y(t) = \underline{\underline{[0.6 - 0.6e^{-2t} \cos(t) - 0.2e^{-2t} \sin(t)]u(t)}}$$

$$(b) \quad x(t) = 6te^{-2t} \longrightarrow X(s) = \frac{6}{(s+2)^2}$$

$$Y(s) = H(s)X(s) = \frac{s+3}{s^2+4s+5} \cdot \frac{6}{(s+2)^2}$$

$$Y(s) = \frac{6(s+3)}{(s+2)^2(s^2+4s+5)} = \frac{A}{s+2} + \frac{B}{(s+2)^2} + \frac{Cs+D}{s^2+4s+5}$$

Equating coefficients :

$$s^3: \quad 0 = A + C \longrightarrow C = -A \quad (1)$$

$$s^2: \quad 0 = 6A + B + 4C + D = 2A + B + D \quad (2)$$

$$s^1: \quad 6 = 13A + 4B + 4C + 4D = 9A + 4B + 4D \quad (3)$$

$$s^0: \quad 18 = 10A + 5B + 4D = 2A + B \quad (4)$$

Solving (1), (2), (3), and (4) gives

$$A = 6, \quad B = 6, \quad C = -6, \quad D = -18$$

$$Y(s) = \frac{6}{s+2} + \frac{6}{(s+2)^2} - \frac{6s+18}{(s+2)^2+1}$$

$$Y(s) = \frac{6}{s+2} + \frac{6}{(s+2)^2} - \frac{6(s+2)}{(s+2)^2+1} - \frac{6}{(s+2)^2+1}$$

$$y(t) = \underline{\underline{[6e^{-2t} + 6te^{-2t} - 6e^{-2t} \cos(t) - 6e^{-2t} \sin(t)]u(t)}}$$

Chapter 16, Solution 33.

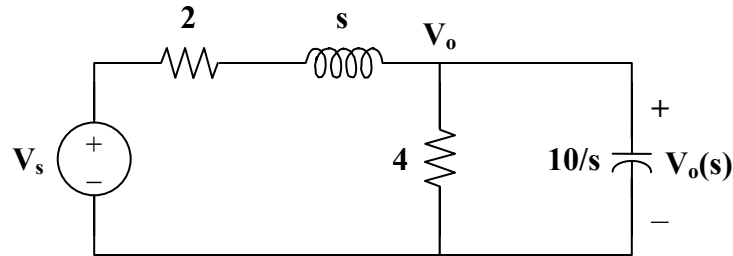
$$H(s) = \frac{Y(s)}{X(s)}, \quad X(s) = \frac{1}{s}$$

$$Y(s) = \frac{4}{s} + \frac{1}{2(s+3)} - \frac{2s}{(s+2)^2+16} - \frac{(3)(4)}{(s+2)^2+16}$$

$$H(s) = sY(s) = \underline{\underline{4 + \frac{s}{2(s+3)} - \frac{2s^2}{s^2+4s+20} - \frac{12s}{s^2+4s+20}}}$$

Chapter 16, Solution 34.

Consider the following circuit.



Using nodal analysis,

$$\frac{V_s - V_o}{s + 2} = \frac{V_o}{4} + \frac{V_o}{10/s}$$

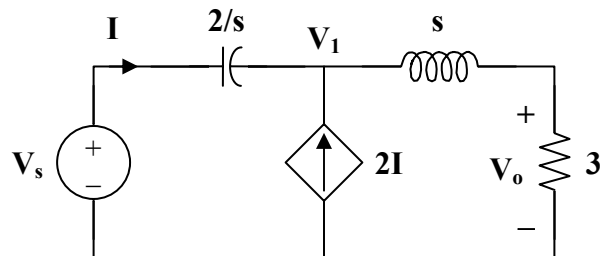
$$V_s = (s + 2) \left(\frac{1}{s + 2} + \frac{1}{4} + \frac{s}{10} \right) V_o = \left(1 + \frac{1}{4}(s + 2) + \frac{1}{10}(s^2 + 2s) \right) V_o$$

$$V_s = \frac{1}{20} (2s^2 + 9s + 30) V_o$$

$$\frac{V_o}{V_s} = \frac{20}{2s^2 + 9s + 30}$$

Chapter 16, Solution 35.

Consider the following circuit.



At node 1,

$$2I + I = \frac{V_1}{s + 3}, \quad \text{where } I = \frac{V_s - V_1}{2/s}$$

$$3 \cdot \frac{V_s - V_1}{2/s} = \frac{V_1}{s+3}$$

$$\frac{V_1}{s+3} = \frac{3s}{2} V_s - \frac{3s}{2} V_1$$

$$\left(\frac{1}{s+3} + \frac{3s}{2} \right) V_1 = \frac{3s}{2} V_s$$

$$V_1 = \frac{3s(s+3)}{3s^2 + 9s + 2} V_s$$

$$V_o = \frac{3}{s+3} V_1 = \frac{9s}{3s^2 + 9s + 2} V_s$$

$$H(s) = \frac{V_o}{V_s} = \frac{9s}{\underline{3s^2 + 9s + 2}}$$

Chapter 16, Solution 36.

From the previous problem,

$$3I = \frac{V_1}{s+3} = \frac{3s}{3s^2 + 9s + 2} V_s$$

$$I = \frac{s}{3s^2 + 9s + 2} V_s$$

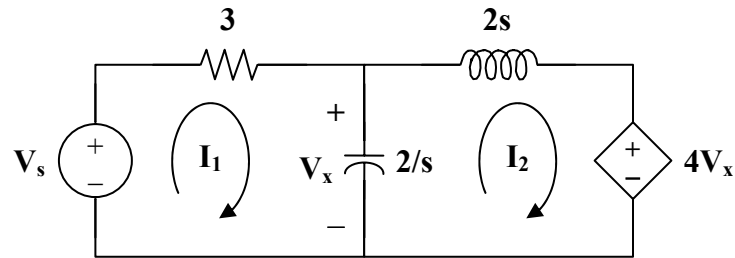
But $V_s = \frac{3s^2 + 9s + 2}{9s} V_o$

$$I = \frac{s}{3s^2 + 9s + 2} \cdot \frac{3s^2 + 9s + 2}{9s} V_o = \frac{V_o}{9}$$

$$H(s) = \frac{V_o}{I} = \underline{9}$$

Chapter 16, Solution 37.

(a) Consider the circuit shown below.



For loop 1,

$$V_s = \left(3 + \frac{2}{s}\right)I_1 - \frac{2}{s}I_2 \quad (1)$$

For loop 2,

$$4V_x + \left(2s + \frac{2}{s}\right)I_2 - \frac{2}{s}I_1 = 0$$

But, $V_x = (I_1 - I_2)\left(\frac{2}{s}\right)$

So, $\frac{8}{s}(I_1 - I_2) + \left(2s + \frac{2}{s}\right)I_2 - \frac{2}{s}I_1 = 0$

$$0 = \frac{-6}{s}I_1 + \left(\frac{6}{s} - 2s\right)I_2 \quad (2)$$

In matrix form, (1) and (2) become

$$\begin{bmatrix} V_s \\ 0 \end{bmatrix} = \begin{bmatrix} 3 + 2/s & -2/s \\ -6/s & 6/s - 2s \end{bmatrix} \begin{bmatrix} I_1 \\ I_2 \end{bmatrix}$$

$$\Delta = \left(3 + \frac{2}{s}\right)\left(\frac{6}{s} - 2s\right) - \left(\frac{6}{s}\right)\left(\frac{2}{s}\right)$$

$$\Delta = \frac{18}{s} - 6s - 4$$

$$\Delta_1 = \left(\frac{6}{s} - 2s\right)V_s, \quad \Delta_2 = \frac{6}{s}V_s$$

$$I_1 = \frac{\Delta_1}{\Delta} = \frac{(6/s - 2s)}{18/s - 4 - 6s} V_s$$

$$\frac{I_1}{V_s} = \frac{3/s - s}{9/s - 2 - 3} = \underline{\underline{\frac{s^2 - 3}{3s^2 + 2s - 9}}}$$

(b) $I_2 = \frac{\Delta_2}{\Delta}$

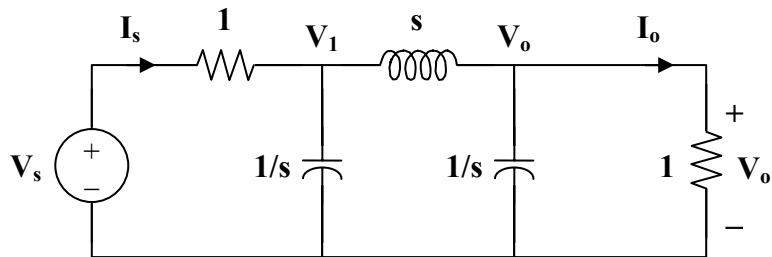
$$V_x = \frac{2}{s} (I_1 - I_2) = \frac{2}{s} \left(\frac{\Delta_1 - \Delta_2}{\Delta} \right)$$

$$V_x = \frac{2/s V_s (6/s - 2s - 6/s)}{\Delta} = \frac{-4V_s}{\Delta}$$

$$\frac{I_2}{V_x} = \frac{6/s V_s}{-4V_s} = \underline{\underline{\frac{-3}{2s}}}$$

Chapter 16, Solution 38.

(a) Consider the following circuit.



At node 1,

$$\frac{V_s - V_1}{1} = sV_1 + \frac{V_1 - V_o}{s}$$

$$V_s = \left(1 + s + \frac{1}{s} \right) V_1 - \frac{1}{s} V_o \quad (1)$$

At node o,

$$\frac{V_1 - V_o}{s} = sV_o + V_o = (s+1)V_o$$

$$V_1 = (s^2 + s + 1)V_o \quad (2)$$

Substituting (2) into (1)

$$V_s = (s+1+1/s)(s^2 + s + 1)V_o - 1/sV_o$$

$$V_s = (s^3 + 2s^2 + 3s + 2)V_o$$

$$H_1(s) = \frac{V_o}{V_s} = \frac{1}{\underline{s^3 + 2s^2 + 3s + 2}}$$

$$(b) \quad I_s = V_s - V_1 = (s^3 + 2s^2 + 3s + 2)V_o - (s^2 + s + 1)V_o$$

$$I_s = (s^3 + s^2 + 2s + 1)V_o$$

$$H_2(s) = \frac{V_o}{I_s} = \frac{1}{\underline{s^3 + s^2 + 2s + 1}}$$

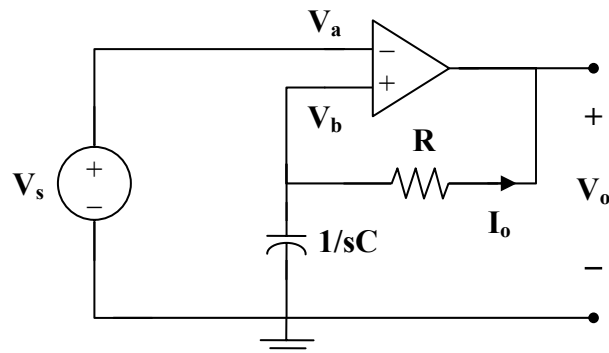
$$(c) \quad I_o = \frac{V_o}{1}$$

$$H_3(s) = \frac{I_o}{I_s} = \frac{V_o}{I_s} = H_2(s) = \frac{1}{\underline{s^3 + s^2 + 2s + 1}}$$

$$(d) \quad H_4(s) = \frac{I_o}{V_s} = \frac{V_o}{V_s} = H_1(s) = \frac{1}{\underline{s^3 + 2s^2 + 3s + 2}}$$

Chapter 16, Solution 39.

Consider the circuit below.



Since no current enters the op amp, I_o flows through both R and C.

$$V_o = -I_o \left(R + \frac{1}{sC} \right)$$

$$V_a = V_b = V_s = \frac{-I_o}{sC}$$

$$H(s) = \frac{V_o}{V_s} = \frac{R + 1/sC}{1/sC} = \underline{\underline{sRC + 1}}$$

Chapter 16, Solution 40.

$$(a) \quad H(s) = \frac{V_o}{V_s} = \frac{R}{R + sL} = \frac{R/L}{s + R/L}$$

$$h(t) = \underline{\underline{\frac{R}{L} e^{-Rt/L} u(t)}}$$

$$(b) \quad v_s(t) = u(t) \longrightarrow V_s(s) = 1/s$$

$$V_o = \frac{R/L}{s + R/L} V_s = \frac{R/L}{s(s + R/L)} = \frac{A}{s} + \frac{B}{s + R/L}$$

$$A = 1, \quad B = -1$$

$$V_o = \frac{1}{s} - \frac{1}{s + R/L}$$

$$v_o(t) = u(t) - e^{-Rt/L} u(t) = \underline{\underline{(1 - e^{-Rt/L}) u(t)}}$$

Chapter 16, Solution 41.

$$Y(s) = H(s)X(s)$$

$$h(t) = 2e^{-t} u(t) \longrightarrow H(s) = \frac{2}{s+1}$$

$$v_i(t) = 5u(t) \longrightarrow V_i(s) = X(s) = 5/s$$

$$Y(s) = \frac{10}{s(s+1)} = \frac{A}{s} + \frac{B}{s+1}$$

$$A = 10, \quad B = -10$$

$$Y(s) = \frac{10}{s} - \frac{10}{s+1}$$

$$y(t) = \underline{\mathbf{10(1 - e^{-t})u(t)}}$$

Chapter 16, Solution 42.

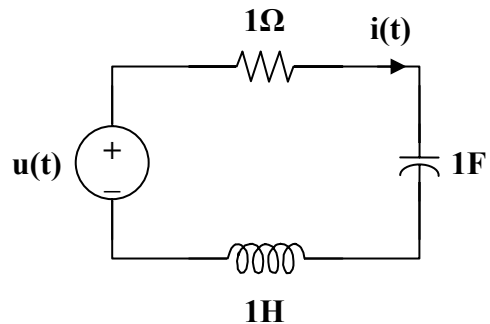
$$2sY(s) + Y(s) = X(s)$$

$$(2s+1)Y(s) = X(s)$$

$$H(s) = \frac{Y(s)}{X(s)} = \frac{1}{2s+1} = \frac{1}{2(s+1/2)}$$

$$h(t) = \underline{\mathbf{0.5e^{-t/2}u(t)}}$$

Chapter 16, Solution 43.



First select the inductor current i_L and the capacitor voltage v_C to be the state variables.

Applying KVL we get:

$$-u(t) + i + v_C + i' = 0; \quad i = v_C'$$

Thus,

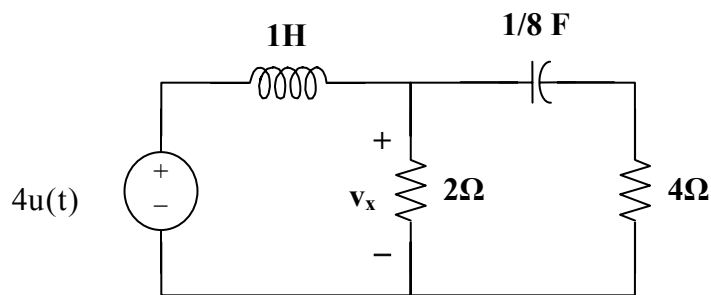
$$v_C' = i$$

$$i' = -v_C - i + u(t)$$

Finally we get,

$$\begin{bmatrix} v_C' \\ i' \end{bmatrix} = \begin{bmatrix} 0 & 1 \\ -1 & -1 \end{bmatrix} \begin{bmatrix} v_C \\ i \end{bmatrix} + \begin{bmatrix} 0 \\ 1 \end{bmatrix} u(t); \quad i(t) = \begin{bmatrix} 0 & 1 \end{bmatrix} \begin{bmatrix} v_C \\ i \end{bmatrix} + \begin{bmatrix} 0 \end{bmatrix} u(t)$$

Chapter 16, Solution 44.



First select the inductor current i_L and the capacitor voltage v_C to be the state variables.

Applying KCL we get:

$$-i_L + \frac{v_x}{2} + \frac{v_C'}{8} = 0; \quad \text{or } v_C' = 8i_L - 4v_x$$

$$i_L' = 4u(t) - v_x$$

$$v_x = v_C + 4 \frac{v_C'}{8} = v_C + \frac{v_C'}{2} = v_C + 4i_L - 2v_x; \quad \text{or } v_x = 0.3333v_C + 1.3333i_L$$

$$v_C' = 8i_L - 1.3333v_C - 5.3333i_L = -1.3333v_C + 2.6666i_L$$

$$i_L' = 4u(t) - 0.3333v_C - 1.3333i_L$$

Now we can write the state equations.

$$\begin{bmatrix} v_C' \\ i_L' \end{bmatrix} = \begin{bmatrix} -1.3333 & 2.666 \\ -0.3333 & -1.3333 \end{bmatrix} \begin{bmatrix} v_C \\ i_L \end{bmatrix} + \begin{bmatrix} 0 \\ 4 \end{bmatrix} u(t); \quad v_x = \begin{bmatrix} 0.3333 \\ 1.3333 \end{bmatrix} \begin{bmatrix} v_C \\ i_L \end{bmatrix}$$